

Calculation Policy



Aims: Here at Kew Riverside, we are enthusiastic, risk-taking mathematicians. Mathematics is a core subject of the National Curriculum and a tool for everyday life. It teaches children to make sense of the world around them through developing their ability to calculate, to reason and to problem solve.

At Kew Riverside, children develop skills, confidence and competence in mathematics. Through a shared ethos of passion and positivity, our children and staff cultivate a love of mathematics and a thirst for knowledge and challenge. Our classroom environments encourage exploration, questioning and mathematical talk as well as opportunities for children to develop and apply their ideas while making connections to the world around them.

By using a 'Maths Mastery Approach' and following the White Rose Primary Scheme of Learning, we ensure pupils develop deep understanding through small steps and opportunities to learn using concrete (manipulatives), pictorial and abstract (written) representations. Pupils who grasp concepts rapidly are challenged with rich and sophisticated problems, in order to prove depth of understanding, before any acceleration through new content. Those who are unable to prove fluency in a concept are given opportunities to consolidate and refine their understanding before moving on.

EYFS (taken from EYFS development matters document 2012 & Statutory framework 2017) Focus during FS2 is developing confidence in recognising numerals, counting accurately with objects, understanding concepts of addition, subtraction, multiplication and division through practical activities and using mathematical vocabulary. By the end of EYFS children should be able to count reliably with numbers from 1 to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer. They solve problems, including doubling, halving and sharing.

Key Stage 1 (taken from the Mathematics Curriculum 2014) The principle focus of mathematics in key stage 1 is to ensure that pupils develop confidence and mental fluency with whole numbers, counting and place value. This should involve working with numerals, words and the four operations, including with practical resources.

By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value.

Lower Key Stage 2 (taken from the Mathematics Curriculum 2014) The principal focus of mathematics teaching in lower key stage 2 is to ensure that pupils become increasingly fluent with whole numbers and the four operations, including number facts and the concept of place value. This should ensure that pupils develop efficient written and mental methods and perform calculations accurately with increasingly large whole numbers.

At this stage, pupils should develop their ability to solve problems, including with decimal place value. By the end of year 4, pupils should have memorised their multiplication tables up to and including the 12 multiplication table and show precision and fluency in their work.

Upper Key Stage 2 (taken from the Mathematics Curriculum 2014) The principle focus of mathematics teaching in upper key stage 2 is to ensure that pupils extend their understanding of the number system and place value to include larger integers. This should develop the connections that pupils make between multiplication and division with fractions, decimals, percentages and ratio.

Problems will demand efficient written and mental methods of calculation. Pupils are introduced to the language of algebra. By the end of year 6, pupils should be fluent in written methods for all four operations, including long multiplication and division.

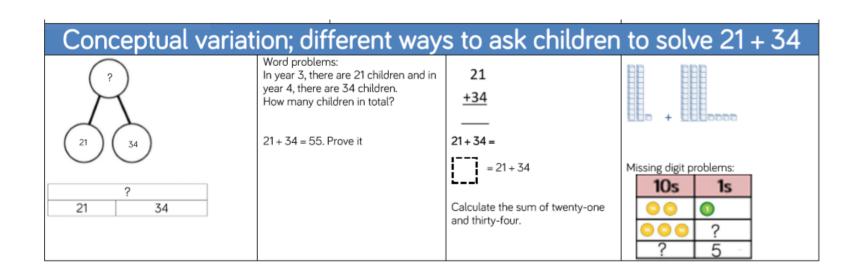


Progression in number lines

EYFS	Number track	Has the numbers inside the sections, rather than on the divisions	0	1		2	3	4	5	6	7	8	9	10	
End of EYF5 and moving towards year 1 expectation	Calibrated, numbered numberline	Equal divisions marked on the numberline and each division is numbered		0	1	2	3	4	4 5	6	7	8	9	10	
Year 1 - National age related expectation	Calibrated, unnumbered numberline	Equal divisions are marked, but left unnumbered for children to add relevant numbers to						Г				_	_		_
Year 2 - National age related expectation	Blank numberline	No divisions or numbers marked for the children		_											_

<u>KS2</u>- Don't underestimate the importance of number lines in KS2. If students understand how to manipulate number lines, they're more likely to succeed throughout KS2 by using number line strategies- especially with mental calculations. Always ask yourself- do you need columns (where simple calculation mistakes can be made) or would it be better on a number line?

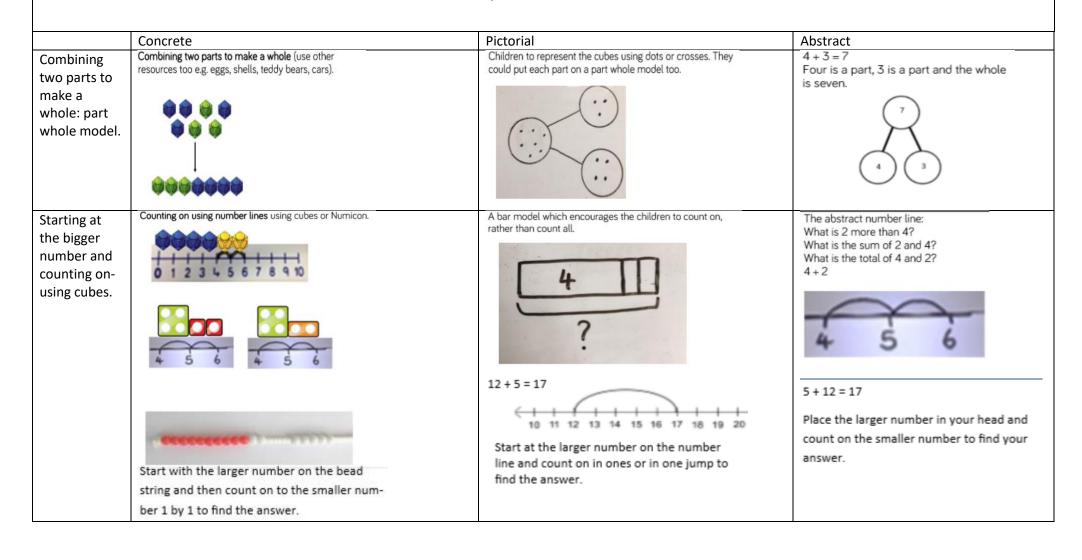
EYFS/Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Combining two parts	Adding three single	Column method-	Column method-	Column method-	Column method-
to make a whole: part whole model.	digits.	regrouping.	regrouping.	regrouping.	regrouping.
Starting at the bigger	Use of base 10 to combine two	Using place value counters	(up to 4 digits)	Use of place value	Abstract methods.
number and counting on- using cubes.	numbers.	(up to 3 digits).		counters for adding decimals.	Place value counters to be used for adding decimal
Regrouping to make 10 using ten frame.					numbers.

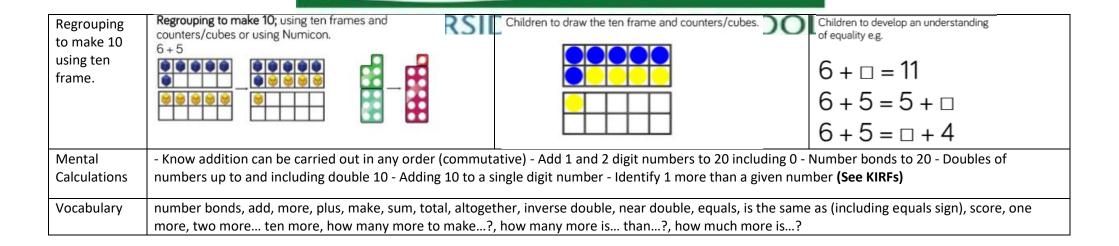




Addition

- read, write and interpret mathematical statements involving addition (+) and equals (=) signs - represent and use number bonds - add one-digit and two-digit numbers to 20, including zero - solve one-step problems that involve addition using concrete objects and pictorial representations, and missing number problems as seem below

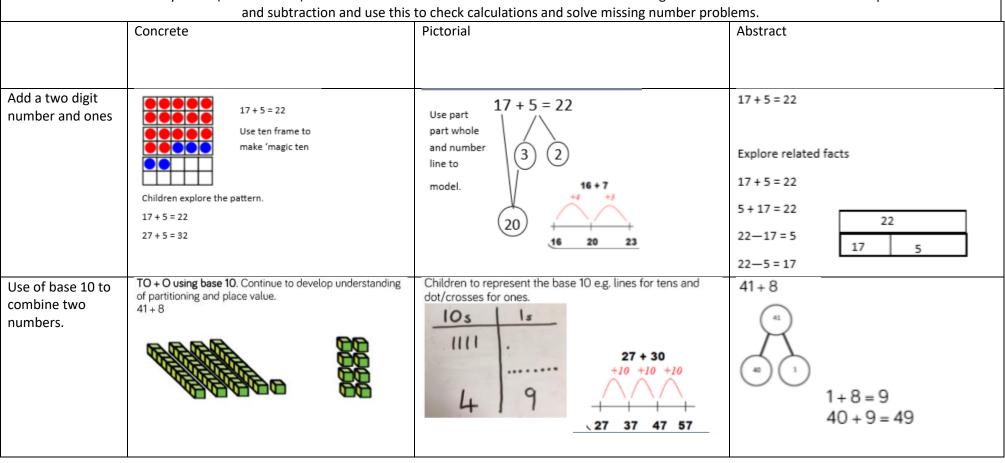


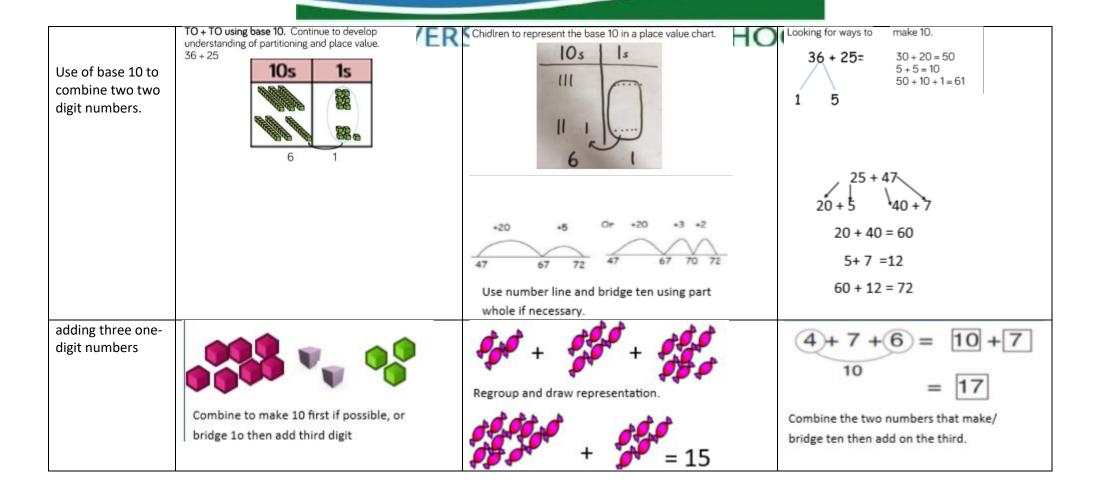


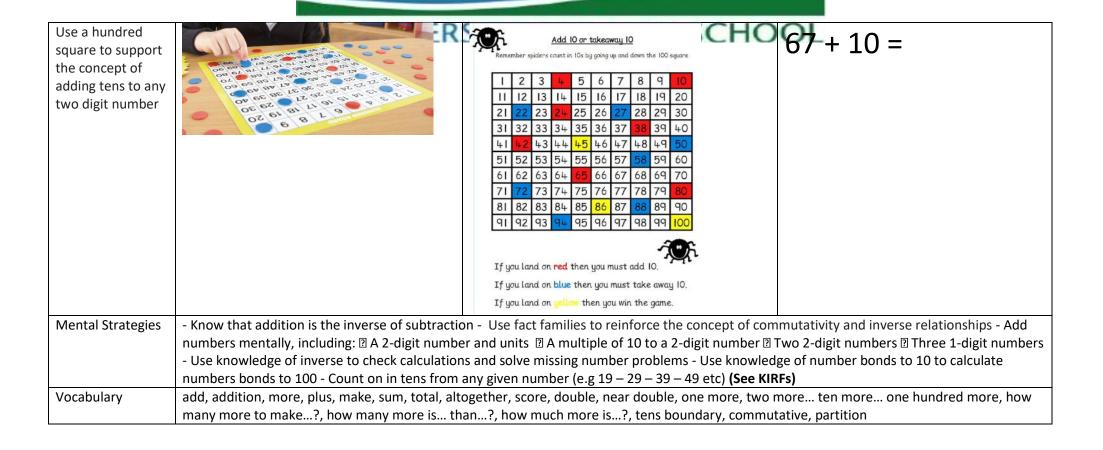


Addition

- solve problems with addition: - using concrete objects and pictorial representations, - applying their increasing knowledge of mental and written methods - recall and use addition facts to 20 fluently, and derive and use related facts up to 100 - add and numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit number and ones - a two-digit number and tens - two two-digit numbers - adding three one-digit numbers - show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot - recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.







Addition

- add and subtract numbers mentally, including: - a three-digit number and ones - a three-digit number and tens - a three-digit number and hundreds - add and subtract numbers with up to three digits, using formal written methods of columnar addition - estimate the answer to a calculation and use inverse operations to check answers - solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction

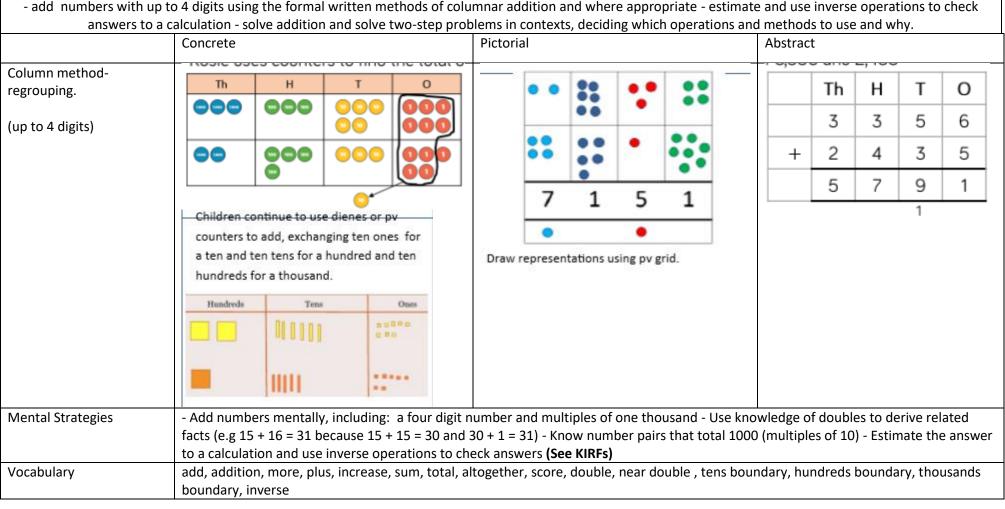
- solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction Concrete **Pictorial** Abstract 353+268=621 Expanded 3 5 6 + 2 1 3 = column addition 300 + 50 + 3→3 0 0 + 5 200 + 60 + 8 2 0 0 + 100 10 Chidren to represent the counters in a place value chart, Use of place value counters to add HTO + TO, HTO + Column 243 circling when they make an exchange. HTO etc. When there are 10 ones in the 1s column- we methodexchange for 1 ten, when there are 10 tens in the 10s 100s 10s regrouping column- we exchange for 1 hundred. 6000 600 00 +368 100s 00 Using 000 place value counters (up to 3 digits).

	KEW RIVERSIDE PRIMARY SCHOOL				
Mental	- Add numbers mentally, including: a three-digit number and a single digit number 🛽 a 3-digit number and multiples of 10 🗈 a 3-digit number and multiples				
Strategies	of 100 - Estimate the answer to a calculation and use inverse operations to check answers - Know number pairs that total 1000 (multiples of 100) -				
	Calculate 10 or 100 more than any given number (See KIRFs)				
Vocabular	add, increase, total, plus, sum, more, altogether, column addition, estimate, inverse, double, near double, one more, ten more one hundred more, how				
У	many more to make? how many more is than? how much more is?, tens boundary, hundreds boundary				



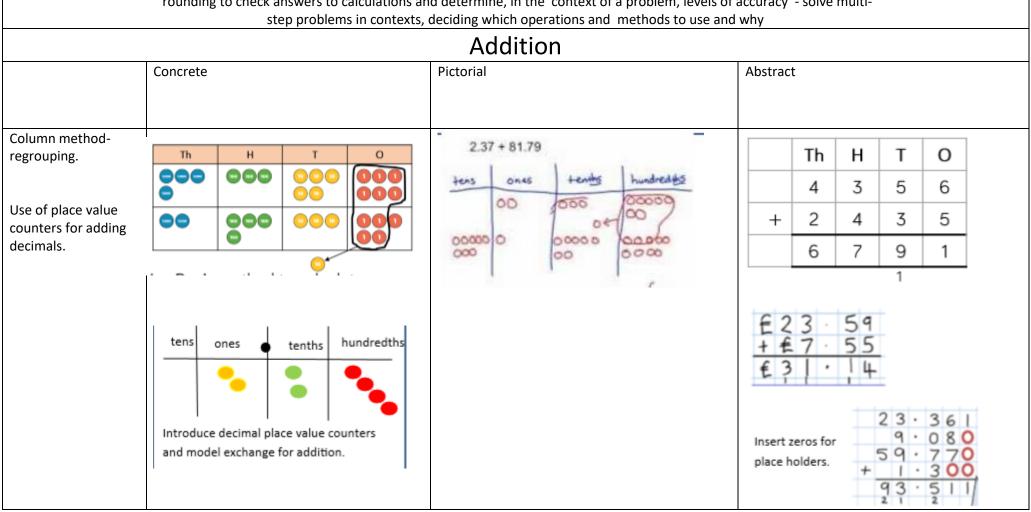
Addition

- add numbers with up to 4 digits using the formal written methods of columnar addition and where appropriate - estimate and use inverse operations to check





- add whole numbers with more than 4 digits, including using formal written methods (columnar addition) - add numbers mentally with increasingly large numbers - use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy - solve multi-



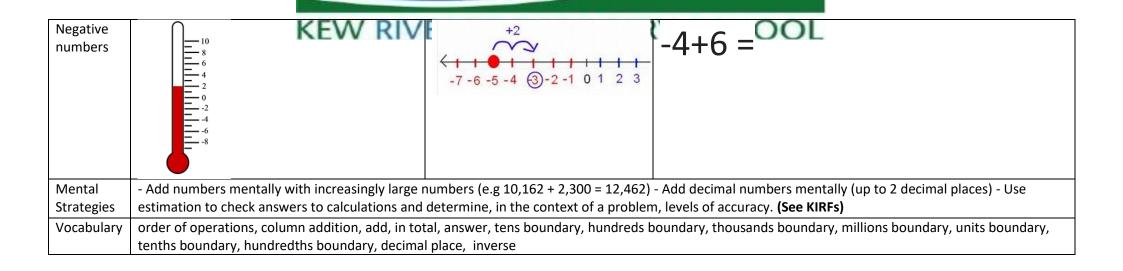
Mental Strategies	- Add numbers mentally with increasingly large numbers (e.g 10,162 + 2,300 = 12,462) - Mentally add tenths (e.g 0.2 + 0.6 = 0.8) and 1-digit whole numbers and tenths (8 + 0.3 = 8.3) - Use number bonds to 100 knowledge to calculate complements to one using hundredths (e.g 0.83 + 0.17 = 1) - Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy (See KIRFs)
Vocabulary	Efficient written method, add, addition, more, plus, increase, sum, total, altogether, score, tens boundary, hundreds boundary, thousands boundary, units boundary, tenths boundary, inverse



Addition

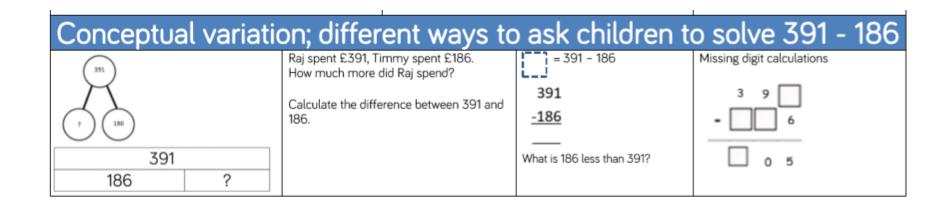
- solve multi-step problems in contexts, deciding which operations and methods to use and why - use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy. Algebra - use simple formulae - express missing number problems algebraically - find pairs of numbers that satisfy an equation with two unknowns

		satisfy an equation with two unknown	lowns
Caliman	Concrete	Pictorial	Abstract
Column method-regrouping . Abstract methods. Place value counters to be used for adding decimal numbers	Tens of Thousands 200 100 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	2.37 + 81.79 tens ones tents hundredts 00 000 0 000 0 000 0 000 0 000 0 000 0 0	23.361+9.08+59.77+1.3=93.511 2 3 3 6 7 7 7





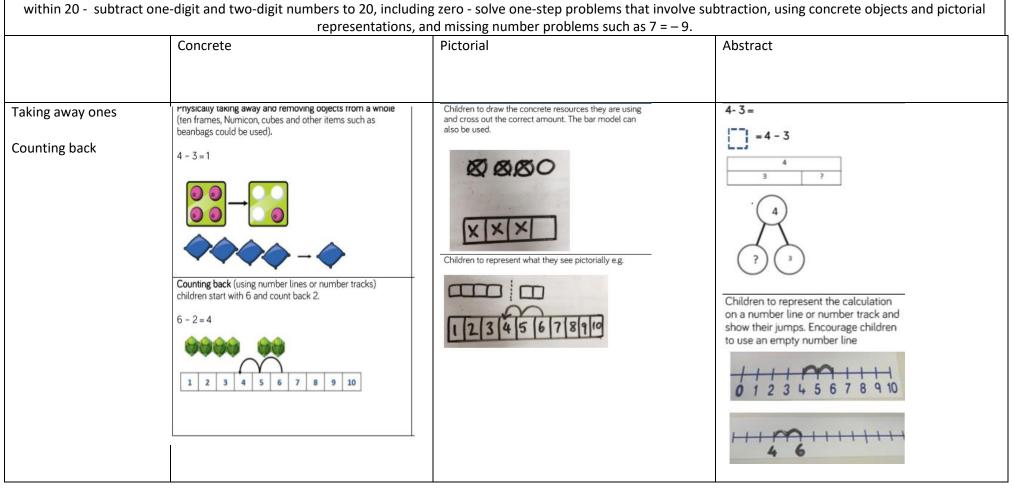
EYFS/Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Taking away ones	Counting back	Column method with regrouping.	Column method with regrouping.	Column method with regrouping.	Column method with regrouping.
Counting back	Find the difference	(up to 3 digits	(up to 4 digits)	Abstract for whole	Abstract methods.
Find the difference	Part whole model	using place value counters)	(05 to 10,810)	numbers.	Place value counters
Part whole model	Make 10	,		Start with place value counters for	for decimals- with different amounts of
Make 10 using the ten frame	Use of base 10			decimals- with the same amount of decimal places.	decimal places.
F	Taking away ones Counting back Find the difference Part whole model Make 10 using the	Counting back Counting back Find the difference Find the difference Part whole model Make 10 Make 10 using the Use of base 10	Counting back Counting back Find the difference Find the difference Counting back Find the difference Find the difference Counting back Find the difference Cup to 3 digits Using place value counters) Make 10 Make 10 Use of base 10	Counting back Counting back Find the difference Find the difference Find the difference Counting back Find the difference Find the difference Part whole model Make 10 Use of base 10 Column method with regrouping. (up to 3 digits using place value counters) Column method with regrouping. (up to 4 digits)	Counting back Counting back Find the difference Find the difference Part whole model Make 10 Use of base 10 Column method with regrouping. Column method with regrouping. Column method with regrouping. Column method with regrouping. (up to 3 digits using place value counters) (up to 4 digits) Abstract for whole numbers. Start with place value counters for decimals- with the same amount of

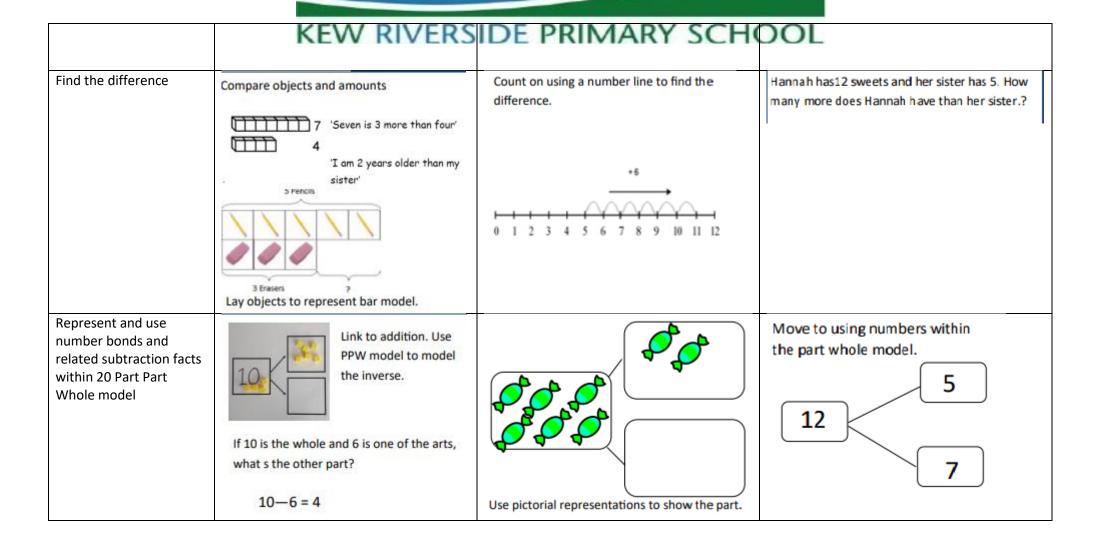




Subtraction

- read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs - represent and use number bonds and related subtraction facts





Make 10 using the ten frame	14-9	13-7	16—8
	Make 14 on the ten frame. Take 4 away to make ten, then take one more away so that you have taken 5.	Jump back 3 first, then another 4. Use ten as the stopping point.	How many do we take off first to get to 10? How many left to take off?
Bar Model		* * * * * * * * * * * * * * * * * * *	8 2
			10 = 8 + 2
			10 = 2 + 8
			10—2 = 8
			10—8 = 2
Mental Strategies	_	uding 0 - To know that subtraction is not community to 10 and 20 to reason (9 + 1 = 10 so 10 – 9 =	
Vocabulary	• • • • • • • • • • • • • • • • • • • •	ny fewer isthan?, how much less is? half, ha ow many fewer is than?, how much less is? e isthan?, how much more is?	

- solve problems with subtraction: - using concrete objects and pictorial representations, including those involving numbers, quantities and measures - applying their in creasing knowledge of mental and written methods - recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100 - subtract numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit number and ones - a two-digit number and tens - two two-digit numbers - show that subtraction has to be done in the order stated - recognise and use the inverse relationship between addition and subtraction and use this to

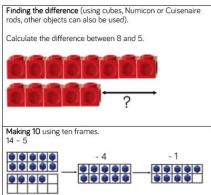
	check cal	culations and solve missing number problems.	
		Subtraction	
	Concrete	Pictorial	Abstract
Regroup a ten into ten ones	Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'	20 – 4 =	20—4 = 16
Partitioning to subtract without regrouping. 'Friendly numbers'	Use Dienes to show how to partition the number when subtracting without regrouping.	Children draw representations of Dienes and cross off.	43—21 = 22

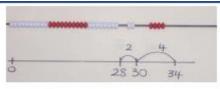
Find the difference

Finding the difference (using cubes, Numicon or Cuisenaire rods, other objects can also be used). Calculate the difference between 8 and 5. Making 10 using ten frames. 14 - 5

Use of base 10

Make 10 **Progression should** be crossing one ten, crossing more than one ten, crossing the hundreds.

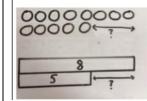




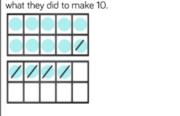
34 - 28

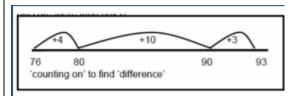
Use a bead bar or bead strings to model counting to next ten and the rest.

Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate.



Children to present the ten frame pictorially and discuss what they did to make 10.





Use a number line to count on to next ten and then the rest.

Find the difference between 8 and 5.

8 - 5, the difference is

Children to explore why 9 - 6 = 8 - 5 = 7 - 4 have the same difference.

Children to show how they can make 10 by partitioning the subtrahend.



14 - 4 = 1010 - 1 = 9

93 - 76 = 17

Mental Strategies	- To know that subtraction is the inverse of addition - Use knowledge of inverse to check calculations and solve missing number problems - Subtract
	numbers mentally, including: 🛽 subtracting units from a 2-digit number 🗈 subtracting a multiple of 10 from a 2-digit number 🗈 subtracting a 2-digit
	number from another 2-digit number - Recall and use subtraction facts to 20 fluently - Use knowledge of number bonds to 100 (multiples of 10) to
	reason $(40 + 60 = 100 \text{ so } 100 - 60 = 40 \text{ and } 100 - 40 = 60)$ (See KIRFs)
Vocabulary	subtract, minus, leave, how many are left/left over?, how many less is than?, how much fewer is?, difference between, half, halve, equals, sign,
	is the same as, partition, inverse, count on, count back, one less, ten less one hundred less.



Subtraction

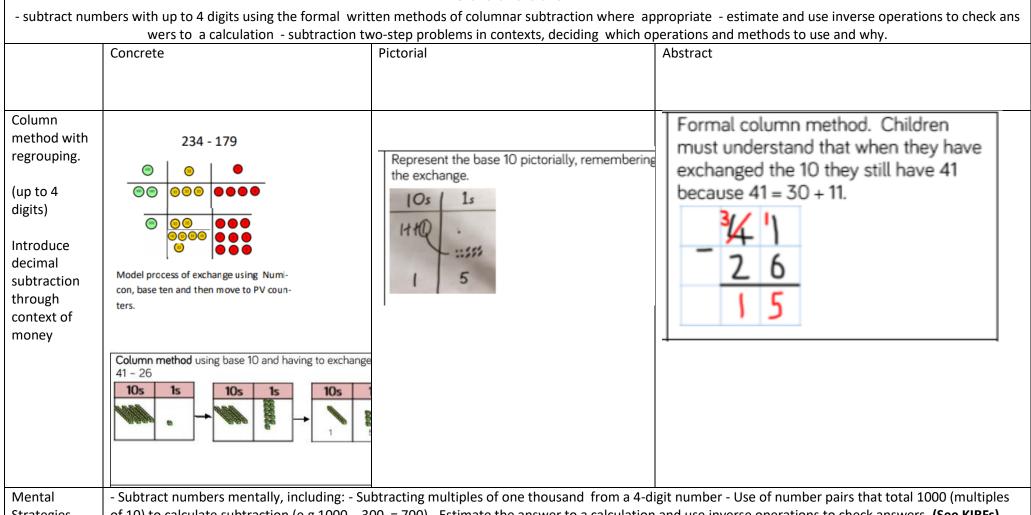
- subtract numbers mentally, including: - a three-digit number and ones - a three-digit number and tens - a three-digit number and hundreds - subtract numbers with up to three digits, using formal written methods of columnar subtraction - estimate the answer to a calculation and use inverse operations to check answers - solve problems, including missing number problems, using number facts, place value, and more complex subtraction.

	Concrete	Pictorial	Abstract
Column subtraction without regrouping (friendly numbers)	Use base 10 or Numicon to model	Darw representations to support understanding	$47-24=23$ $-\frac{40+7}{20+4}$ Intermediate step may be needed to lead to clear subtraction understanding. 32 -12 20
Column method with regrouping. (up to 3 digits using place value counters)	Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into tten ones. Use the phrase 'take and make' for exchange.	Tens 10 nes Tens	836-254=582 300 130 6 Begin by partitioning into pv columns 728-582=146 Then move to formal method. 7 12 8 5 8 2 1 4 6 7 12 8 5 8 2 1 4 6 836-254=582 146 Then move to formal method.

Mental Strategies	- Subtract numbers mentally, including: 2 Subtracting a single digit number from a 3-digit number 2 Subtracting a multiple of 10 from a 3-digit number. Subtracting a multiple of 10 from a 3-digit number - Estimate the answer to a calculation and use inverse
	operations to check answer (See KIRFs)
Vocabulary	leave, subtract, less, minus, column subtraction, inverse, decomposition, exchange, how many are left/left over?, difference
	between, how many more/fewer is than?, how much more/less is?, Is the same as, equals, sign. multiples of tens and
	hundreds.



Subtraction



Strategies

of 10) to calculate subtraction (e.g 1000 – 300 = 700) - Estimate the answer to a calculation and use inverse operations to check answers. (See KIRFs)

Vocabulary	subtract, subtraction, minus, decrease, leave, how many are left/left over?, difference between, how many more/fewer is than?, how much
	more/less is?, Is the same as, equals, sign. Column subtraction, decomposition, exchange, multiples of thousand, inverse,



Year 5 Subtraction - subtract whole numbers with more than 4 digits, including using formal written methods - subtract numbers mentally with increasingly large numbers - use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy - solve multistep problems in contexts, deciding which operations and methods to use and why. Concrete **Pictorial** Abstract Column method with Column method using place value counters. Represent the place value counters pictorially; Formal colum method. 234 - 88regrouping. remembering to show what has been exchanged. understand what has ha 100s 10s they have crossed out of 105 1005 Abstract for whole numbers. 000 0000 OØ Start with place value counters for decimals- with the same amount of decimal places **Mental Strategies** - Subtract increasingly large numbers mentally (e.g 12, 654 - 1, 341 = 11, 213) - Mentally subtract tenths (e.g 0.7 - 0.5 = 0.2) and 1-digit whole numbers and tenths (8 - 0.3 = 7.7) - Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy (See KIRFs) efficient written method, subtract, subtraction, minus, decrease, difference between, inverse, decimals, units and tenths boundary, Vocabulary column subtraction, decomposition, exchange.



Subtraction

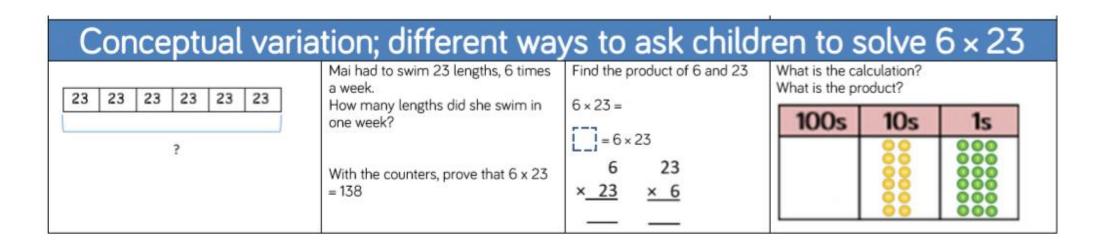
- perform mental calculations, including with mixed operations and large numbers - use their knowledge of the order of operations to carry out calculations involving th e four operations - solve multi-

step problems in contexts, deciding which operations and methods to use and why - use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy. Algebra - use simple formulae - express missing number problems algebraically - find pairs of numbers that satisfy an equation with two unknowns

							•	ation v	.wo unknowns	
	Concrete								Pictorial	Abstract
Column method with regrouping.	Tens of Thousands 10,000	Thousands	Hundreds 100	Tens.	Ones 1	Decimal point	Tenths 1 10 0.1	Hundredths 1 100 0.01		This will lead to an understanding of
Abstract methods.										subtracting any number including decimals.
Place value counters for decimals- with different amounts of decimal places.										$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
Mental Strategies	- Subtract increasingly large numbers mentally (e.g 12, 654 – 1,341 = 11, 213) - Subtract decimal numbers mentally (up to 2 decimal places) - Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy. (See KIRFs)									
Vocabulary	order of operations, subtract, decrease, difference, inverse, decimals, units, tenths and hundredths boundary, column subtraction, decomposition, exchange.									



_	EYFS/Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Multiplication	Recognising and making equal groups. Doubling Counting in multiples Use cubes, Numicon and other objects in the classroom	Arrays- showing commutative multiplication	Arrays 2d × 1d using base 10	Column multiplication- introduced with place value counters. (2 and 3 digit multiplied by 1 digit)	Column multiplication Abstract only but might need a repeat of year 4 first(up to 4 digit numbers multiplied by 1 or 2 digits)	Column multiplication Abstract methods (multi-digit up to 4 digits by a 2 digit number)





		EYFS/ Year 1	
		Multiplication	
- solve one-	step problems involving multiplication by calculating Concrete	the answer using concrete objects, pictorial represent Pictorial	Abstract
Doubling	Use practical activities using manipultives including cubes and Numicon to demonstrate doubling	Double 4 is 8	Partition a number and then double each partition before recombining it back together. 16 10 6 1x2 1x2 20 + 12 = 32

Recognising and making equal groups.

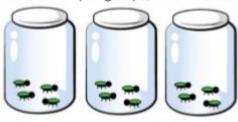
Counting in multiples Use cubes, Numicon and other objects in the classroom

Repeated grouping/repeated addition

 3×4

4 + 4 + 4

There are 3 equal groups, with 4 in each group.









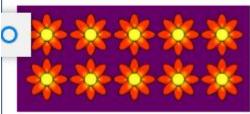
Number lines to show repeated groups- 3×4



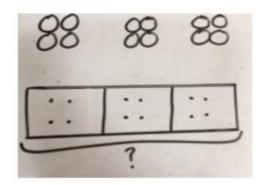


Cuisenaire rods can be used too.

Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.



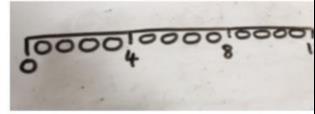
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$$3 \times 4 = 12$$

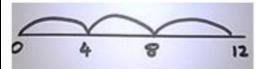
$$4 + 4 + 4 = 12$$

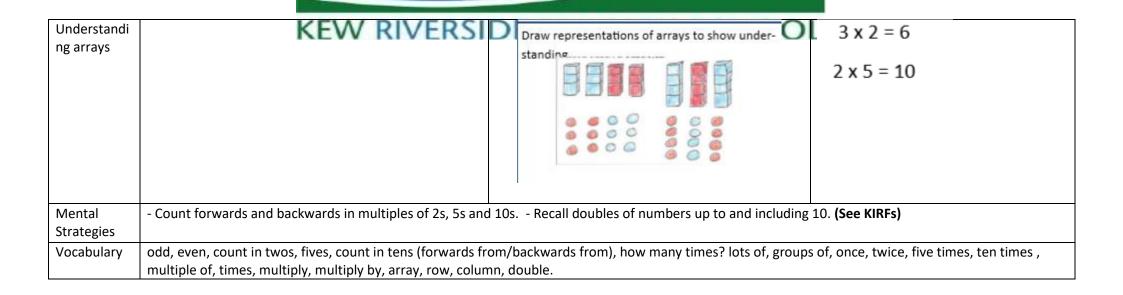
Represent this pictorially alongside a number line



Abstract number line showing three jum of four.

$$3 \times 4 = 12$$







Multiplication

- recall and use multiplication facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers - calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (x) and equals (=) signs - show that multiplication of two numbers can be done in any order (commutative) - solve problems involving multiplication using materials, arrays, repeated addition, mental methods, and multiplication facts, including problems in contexts.

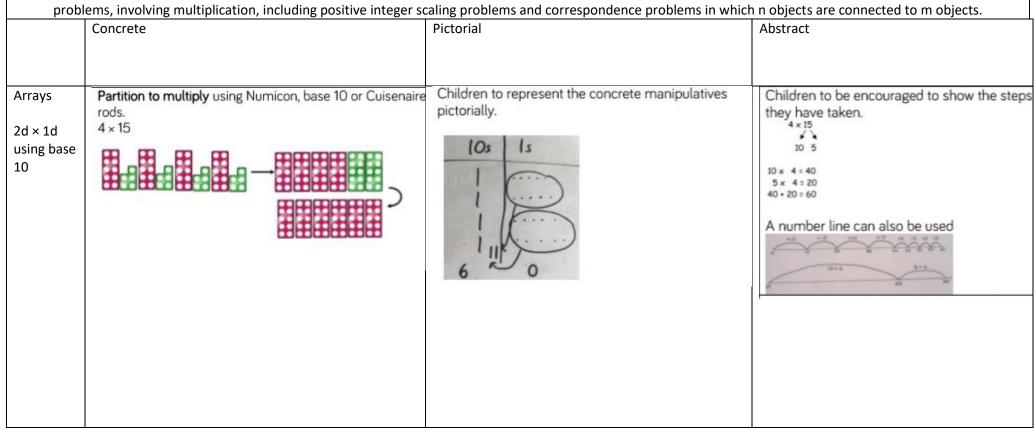
	Concrete	problems in contexts. Pictorial	Abstract
	Concrete	rictorial	Abstract
howing ommutative nultiplication	Use arrays to illustrate commutativity counters and other objects can also be used. 2 × 5 = 5 × 2 2 lots of 5 5 lots of 2	Children to represent the arrays pictorially.	Children to be able to use an array to write a range of calculations e.g. $10 = 2 \times 5$ $5 \times 2 = 10$ $2 + 2 + 2 + 2 + 2 = 10$ $10 = 5 + 5$
	Create arrays using counters, cubes to show multiplication sentences. $4 \times 6 = 24$ Begin to look at arrays in different orientations to make the link between, for example, $5 \times 3 = 15$ and $3 \times 5 = 15$ (commutativity)	Draw arrays in different rotations to find commutative multiplication sentences. 000 4×2=8 2×4=8 000 4×2=8 Link arrays to area of rectangles.	Use an array to write multiplication sentences and reinforce repeated addition. 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15

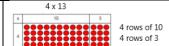
Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.	VERS O O O O	8 x =	2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8 ÷ 2 Show all 8 related fact family sentences.			
Mental Strategies	- Count forwards and backwards in multiples of 3 Kno KIRFs)	ow the 2, 5 and 10 times tables (in ar	nd out of order) - Recognise odd and even numbers (See			
Vocabulary	odd, even, twos, fives, tens, threes, lots of, groups of, once, twice, three times, five times, ten times, multiple of, times, multiply, multiply by, repeated addition, array, row, column, double.					
Times Tables	2, 5, 10					



Multiplication

- recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables - write and calculate mathematical statements for multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods - solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.





Move on to using Dienes to move towards a more compact method



4 rows of 13

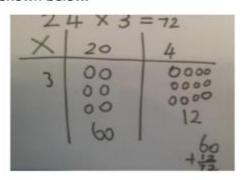
Move on to place value counters to show how we are finding groups of a number.



We are multiplying by 4 so we need 4 rows with each containing 26.

V RIVERS Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.



Bar model are used to explore missing numbers

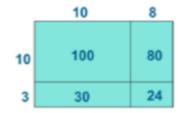
Start with multiplying 2digit by 1-digit numbers showing the addition alongside the grid.

×	30	5
7	210	35

210 + 35 = 245

Moving forward, multiply 2, 3 and 4-digit numbers showing the different rows within the grid method.

	13 X	28	
Х	20	8	
10	200	80	280
3	60	24	+ 84
			364
			1



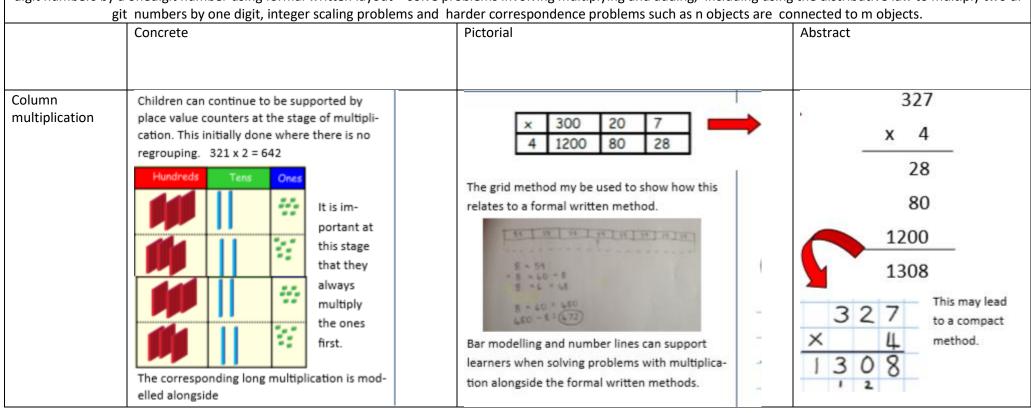
Mental	- Count forwards and backwards in multiples of 4, 8, 50 & 100 - Know the 3, 4 and 8 times tables (in a
Strategies	nd out of order) - Connect the 2, 4 and 8 times tables through doubling - Use knowledge of place value to calculate multiplication (e.g. 2 x 2 = 4, 2 x 20 = 40,
	2 x 200 = 400) (See KIRFs)
Vocabular	multiply, times, groups of, equal groups of, multiple of, multiplied by, estimate, inverse, grid multiplication, expanded column multiplication, partition,
У	commutative, associative, product.
Times	Consolidate- 2, 5, 10
Tables	Learn- 3, 4, 8



Multiplication

- recall multiplication tables up to 12 × 12 - use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three n umbers - recognise and use factor pairs and commutativity in mental calculations - multiply two-digit and three-

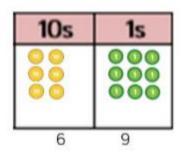
digit numbers by a onedigit number using formal written layout - solve problems involving multiplying and adding, including using the distributive law to multiply two di



Column multiplicationintroduced with place value counters.

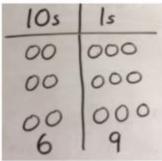
(2 and 3 digit multiplied by 1 digit)

Formal column method with place value counters] Children to represent the counters pictorially. (base 10 can also be used.) 3 x 23

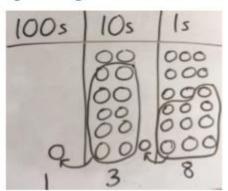


Formal column method with place value counters. 6 x 23

100s	10s	1s
	000000	000 000 000 000
	-	
100s	10s	1s



Children to represent the counters/base 10, pictorial e.g. the image below.



For 38 x 7

38 56 8 x 7 210 30 x 7 266

Children to record what it is they are doing to show understanding.

$$3 \times 23$$
 $3 \times 20 = 60$
 $/ \setminus 3 \times 3 = 9$
 $20 \ 3 \ 60 + 9 = 69$

23

Formal written method

$$6 \times 23 =$$

Mental Strategies

- Know all times tables up to and including 12 x 12 (by the end of Year 4) - Recognise and use factor pairs (e.g factor pairs for numbers up to and including 10) - Know that TU x 5 is TU x 10 then divide by 2 (e.g 18 x 5 = $(18 \times 10) \div 2 = 90$) - Know that TU x 9 is TU x 10 then subtract TU (e.g 18 x 9 = $(18 \times 10) - 18 = 162)$ (See KIRFs)

Vocabulary

multiply, multiplied by, product, short multiplication, partition, distributive law, commutative, groups of, multiply, times, multiples, inverse.

	and the second commence of the second commenc
Times Tables Consolidate- 2, 5, 10 (yr 2) 3, 4, 8 (yr 3)	INVADA CCHUUI
Consolidate 2, 3, 10 (vi 2) d, 4, 8 (vi 3)	IIVIAKI SCHOOL
Learn- 6, 7, 9, 11, 12	



Multiplication

- identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers - know and use the vocabulary of prime numbers, prime factors and composite (non-

prime) numbers - establish whether a number up to 100 is prime and recall prime numbers up to 19 - multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-

digit numbers - multiply numbers mentally drawing upon known facts - multiply and whole numbers and those involving decimals by 10, 100 and 1000 recognise and u se square numbers and cube numbers, and the notation for squared (2) and cubed (3) - solve problems involving multiplication including using their knowledge of facto rs and multiples, squares and cubes - solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign - solve problems involving multiplication and division, including scaling by simple fractions and problems involving

e meaning of the	Concrete	Pictoria		0 - 1	 bstract				- 0
Column multiplication		_							
Abstract only but might		×	40	4			2	3	
need a repeat of year 4 first(up to 4 digit numbers		30	1,200	120	×		1	4	
multiplied by 1 or 2 digits)							9	2	(23×4)
	Whitney uses Base 10 to calculate 23 × 22	2	80	8		2	3	0	(23×10)
	→ 400 40								
	60 6								

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Mental Strategies	- Recognise and calculate factor pairs for any number - Use times table knowledge to derive multiples of any number - Establish whether a number is a prime number (up to 100) or a composite number (not prime) and recall prime numbers up to 19 - To know what a square number is and recall all square numbers (up to and including 144) - To know what a cube number is and recall the first 5 cube numbers (See KIRFs)
Vocabulary	composite numbers, prime number, prime factor, cube number, square number, derive, factor pairs, formal written method, times, multiply, multiplied by, multiple of, product, short multiplication, partition, long multiplication, scaling, decimal place, units, tenths and hundreds.
Times Tables	Know all times tables up to and including 12 x 12 and related division facts



Multiplication

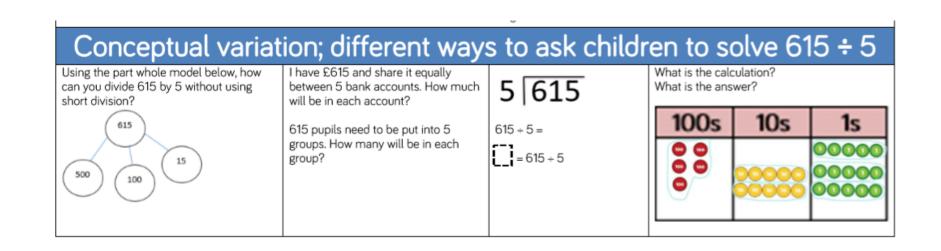
- multiply multi-digit numbers up to 4 digits by a two

digit whole number using the formal written method of long multiplication - perform mental calculations, including with mixed operations and large numbers - identify common factors, common multiples and prime numbers - use their knowledge of the order of operations to carry out calculations involving the four operations - use es timation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy. Ratio & Proportion - solve problems involving the relative sizes of two quantities where missing values can be found by using integer - multiplication and division facts - solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison - solve problems involving similar shapes where the scale fact or is known or can be found - solve problems involving unequal sharing and grouping using knowledge of fractions and multiples. Algebra - use simple formulae - express missing number problems algebraically - find pairs of numbers that satisfy an equation with two unknowns

	Concrete			Pictorial	Abstract
Column multiplication Abstract methods (multi-digit up to 4 digits by a 2 digit number)	2 3 1	7 4 4 8 2 2	2 4 2 6 1 4 3 0 2 4	When children start to multip To get 744 children have solve To get 2480 they have solve	

Multiplying decimals up to 2 decimal places by a single digit.	Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer. 3 1 9 × 8 2 5 · 5 2
Mental Strategies	- Use scaling to solve decimal number problems as whole number problems using the rule: 'the number of decimal digits in the question is the same as the number of decimal digits in the answer' - Identify common factors, common multiples and prime numbers - Use common factors to simplify fractions mentally - Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy (See KIRFs)
Vocabulary	common factors, multiples, prime, formal written method, multiply, multiplied by, multiple of, product, short and long multiplication, partition, scaling, decimal place, units, tenths and hundreths.
Times Tables	Know all times tables up to and including 12 x 12 and related division facts/ powers/ square roots/ BODMAS

EYFS/Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Sharing objects into	Division as	Division with a	Division with a	Short division	Short division
groups	grouping	remainder-using	remainder		
District	Di ini ana salah	lollipop sticks,	Charles 1: 1: 1: (1: - 7	(up to 4 digits by a	Long division with
Division as grouping e.g. I have 12 sweets	Division within	times tables facts	Short division (up to 3 digits by 1 digit-	1 digit number including	place value counters
and put them in	arrays- linking to multiplication	and repeated subtraction.	concrete and pictorial)	remainders)	(up to 4 digits by a 2 digit number)
groups of 3, how	monipheation	Sooti action.	concrete and pictorial)	remainders)	olgit Horricer)
many groups?	Repeated	2d divided by 1d			Children should
, , ,	subtraction	using base 10 or			exchange into the
Use cubes and draw		place value			tenths and
round 3 cubes at a		counters			hundredths column
time.					too



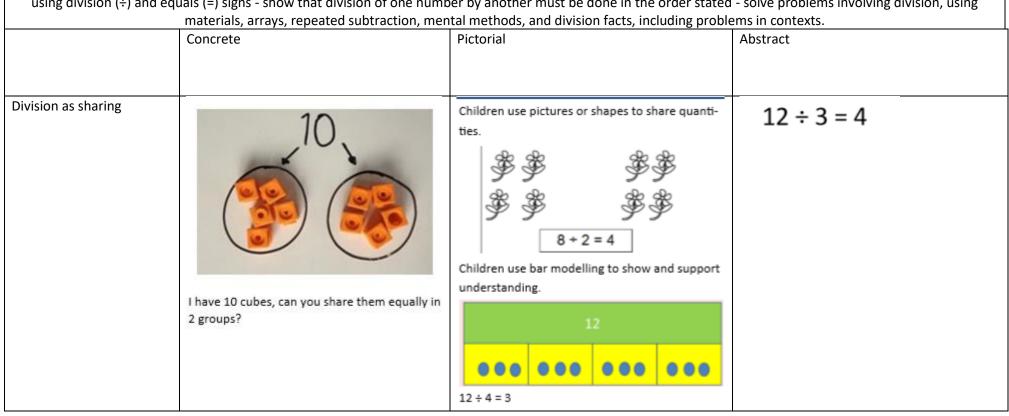


		EYFS/ Year 1	
		Division	
- solve one-step problems involvi	ng division, by calculating the answ Concrete	ver using concrete objects, pictorial representa Pictorial	Abstract
Division as grouping e.g. I have 12 sweets and put them in groups of 3, how many groups? Use cubes and draw round 3 cubes at a time.	Sharing using a range of objects. 6 + 2	Represent the sharing pictorially.	6 ÷ 2 = 3 Children should also be encouraged to use their 2 times tables facts.
Mental Strategies	Count forwards and backwards i	n multiples of 2s, 5s and 10s. (See KIRFs)	
Vocabulary	halve, share, share equally, grou	ps, equal groups of, divide, divided by, left, lef	t over



Division

- recall and use division facts for the 2, 5 and 10 multiplication tables - calculate mathematical statements for division within the multiplication tables and write them using division (÷) and equals (=) signs - show that division of one number by another must be done in the order stated - solve problems involving division, using materials, arrays, repeated subtraction, mental methods, and division facts, including problems in contexts.

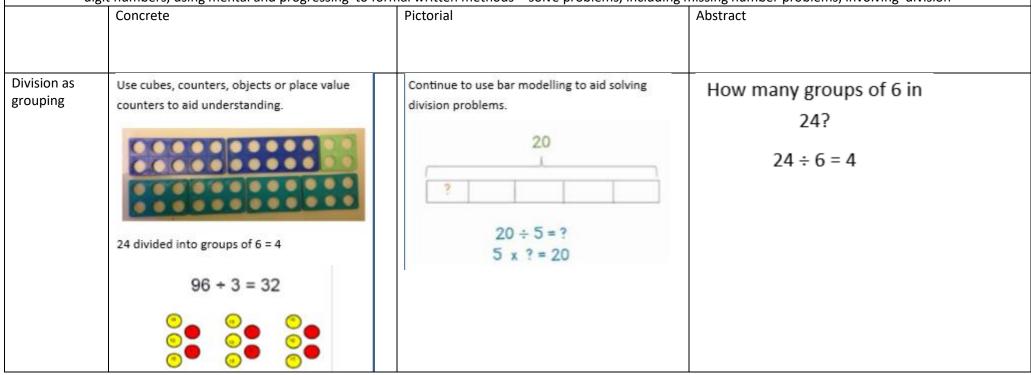


Division as grouping	Repeated subtraction using Cuisenaire rods above a ruler. 6 + 2 Children to represent repeated subtraction pictorially. Abstract number line to represent the equation groups that have been subtracted.
Division within arrays- linking to multiplication Repeated subtraction	3 groups of 2
Mental Strategies	- To know that division is the inverse of multiplication - Recall division facts for the 2, 5 and 10 times tables - Recall halves for even numbers up to and including 2 (See KIRFs)
Vocabulary	groups of, equal groups of, halve, share, share equally, divide, divided by, divided into, repeated subtraction, inverse.

Division

- recall and use division facts for the 3, 4 and 8 multiplication tables - write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-

digit numbers, using mental and progressing to formal written methods - solve problems, including missing number problems, involving division



Division with arrays



Link division to multiplication by creating an array and thinking about the number sentences that can be created.

Eg 15 ÷ 3 = 5 5 x 3 = 15

15 ÷ 5 = 3 3 x 5 = 15

Praw an array and use lines to split the array into groups to make multiplication and division sentences



















Find the inverse of multiplication and division sentences by creating eight linking number sentences.

 $7 \times 4 = 28$

 $4 \times 7 = 28$

 $28 \div 7 = 4$

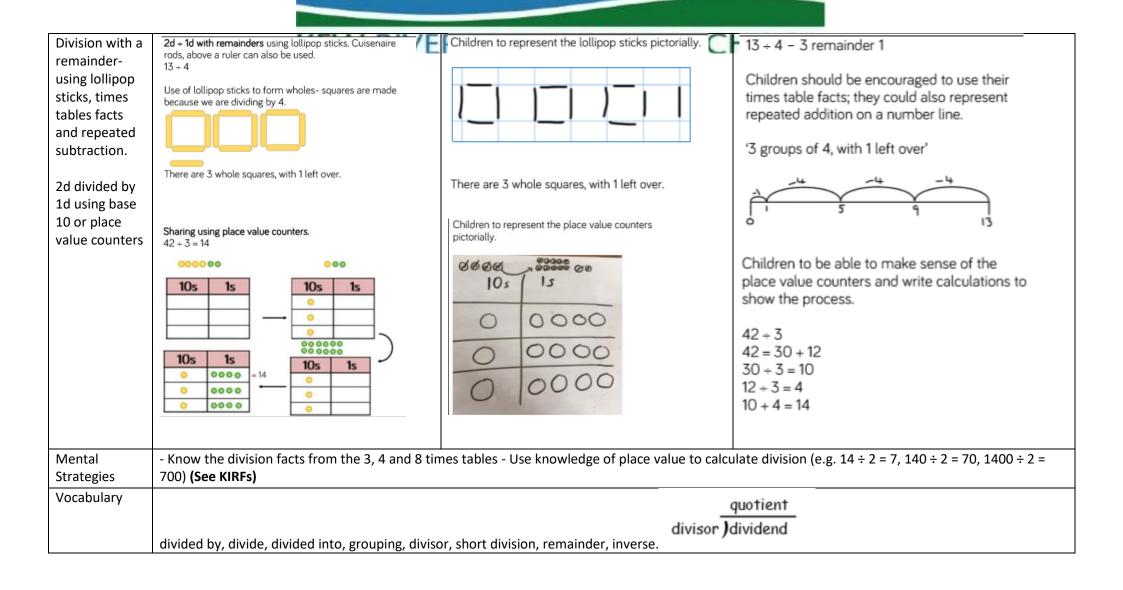
 $28 \div 4 = 7$

 $28 = 7 \times 4$

 $28 = 4 \times 7$

 $4 = 28 \div 7$

 $7 = 28 \div 4$





Year 4 Division - recall division facts for multiplication tables up to 12 × 12 - use place value, known and derived facts to divide mentally, including: dividing by 1; Concrete **Pictorial** Abstract Represent the place value counters pictorially. Children to the calculation using the short Division with a remainder Short division using place value counters to group. 615 ÷ 5 division scaffold. 1005 Short division (up to 3 10s 100s 15 digits by 1 digit- concrete 00 00000 00 and pictorial) 00000 1. Make 615 with place value counters. 2. How many groups of 5 hundreds can you make with 6 hundred counters? 3. Exchange 1 hundred for 10 tens. 4. How many groups of 5 tens can you make with 11 ten counters? 5. Exchange 1 ten for 10 ones. 6. How many groups of 5 ones can you make with 15 ones?

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	Know all related division facts for all times tables up to 12 times table (by the end of Year 4) (See KIRFs)
Mental Strategies	
Vocabulary	factor, divisor, divided by, divided into, remainders, divisible by, equivalent, short division, derive, Quotient, inverse, remainder,
	divisor dividend multiples, exchange. Division bracket



Division

- divide numbers mentally drawing upon known facts - divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context - divide whole numbers and those involving decimals by 10, 100 and 1000 - solve problems involving, squares and cubes - solve problems involving addition, subtraction, multiplication and division and a combination of these, - solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates.

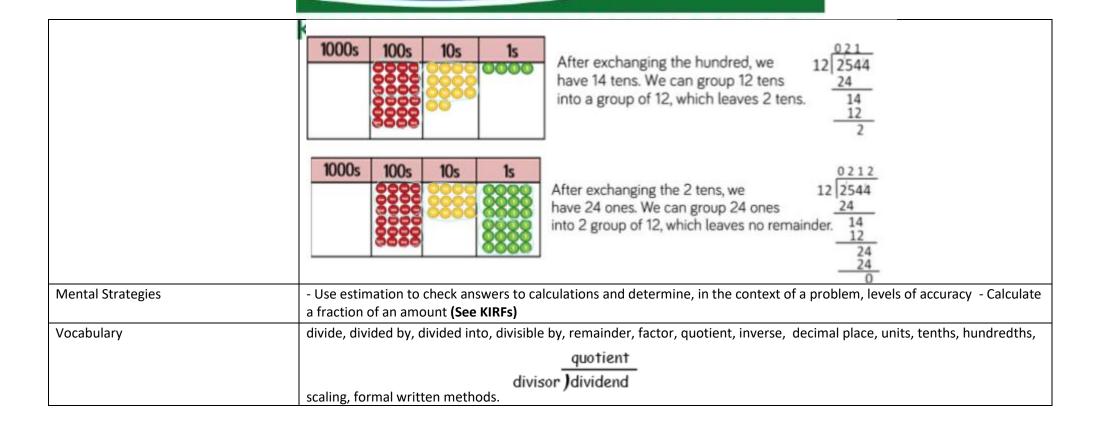
	Concrete	Pictorial	Abstract
Short division (up to 4 digits by a 1 digit number including remainders)	9635÷3 =		9635÷3 = 3211 r ² 3 9635
	3/ 1033		Group the units counters according to the divisor and write the number of groups about the line in the units column. Express remainders as 'r2' as part of the quotient.
Mental Strategies	- Multiply and divide numbers n	nentally drawing upon known f	facts - Associate fractions with division (See KIRFs)
Vocabulary		divisible by, remainder, quotie <u>quotient</u> divisor) dividend	ent, inverse, decomposing, factor, decimal place, units,



Division

- divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and - - interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context - divide numbers up to 4 digits by a two-digit number using the formal written method of short division where - - - appropriate, interpreting remainders according to the context - perform mental calculations, including with mixed operations and large numbers - use their knowledge of the order of operations to carry out calculations involving the four operations - solve problems involving addition, subtraction, multiplication and division - use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy. Ratio & Proportion - solve problems involving the relative sizes of two quantities where missing values can be found by using integer - multiplication and division facts - solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison - solve problems involving similar shapes where the scale factor is known or can be found - solve problems involving unequal sharing and grouping using knowledge of fractions and multiples.

Algebra - use simple formulae -				•	raically - find pairs of numbers that satisf	9	•
Short division	Long divis	2.9	g place v	alue coun	ters		
Long division with place value counters (up to 4 digits by a 2 digit number) Children should exchange into the	2544 + 12	100s	10s	1s 0000	We can't group 2 thousands into groups of 12 so will exchange them.		
tenths and hundredths column too	1000s	100s	10s	1s	We can group 24 hundreds into groups of 12 which leaves with 1 hundred.	12 2544 24 1	





Key Instant Recall Facts (KIRFs)

By the end of an academic year, pupils should be able to recall the **Key Instant Recall Facts** for their year group quickly (within 5 seconds) and complete counting activities confidently and fluently. Children should also be able to recall the **Key Instant Recall Facts** for all previous year groups within the same amount of time.

Year 1	Autumn 1	I know number bonds to 6	
	Autumn 2	I can count in 2s, 5s and 10s	
	Spring 1	I know doubles and halves of numbers to 10	
	Spring 2	I know number bonds to 10	
	Summer1	I know the days, weeks, months and seasons.	
	Summer 2	I know my number bonds for each number to 10	
Year 2	Autumn 1	I know number bonds to 20.	
	Autumn 2	I know the multiplication and division facts for the 2 times table.	
	Spring 1	I know double and halves to 20	
	Spring 2	I know the multiplication and division facts for the 10 times table.	
	Summer1	I can tell the time to the nearest 5 minutes	
	Summer 2	I know the multiplication and division facts for the 5 times table.	



Year 3	Autumn 1	I know number bonds for all numbers to make 20.		
	Autumn 2	I know the multiplication and division facts for the 3 times table.		
	Spring 1	I can recall facts about durations in time.		
	Spring 2	I know the multiplication and division facts for the 4 times table.		
	Summer1	I can tell the time to the nearest minute.		
	Summer 2	I know the multiplication and division facts for the 8 times table.		
Year 4	Autumn 1	I know number bonds for all numbers to make 100.		
	Autumn 2	I know the multiplication and division facts for the 6 times table.		
	Spring 1	I know the multiplication and division facts for the 9 and 11 times tables.		
	Spring 2	I can recognise decimal equivalents of fractions.		
	Summer1	I know the multiplication and division facts for the 7 times table.		
	Summer 2	I can multiply and divide single-digit numbers by 10 and 100.		
Year 5	Autumn 1	I know decimal number bonds 10 1 and 10		
	Autumn 2	I know multiplication and division facts up to 12 x12		
	Spring 1	I can recall metric conversions.		
	Spring 2	I can identify prime numbers up to 20		
	Summer 1	I can recall square numbers up to 12 squared and their square roots.		
	Summer 2	I can find factor pairs of a number.		
Year 6	Autumn 1	I know multiplication and division facts up to 12 x12		

Autumn 2	I can identify common factors of a pair of numbers.
Spring 1	I can convert between decimals, fractions and percentages.
Spring 2	I can identify prime numbers up to 50
Summer1	Consolidation
Summer 2	Consolidation

Topic	Facts taught in this year group	Facts taught in previous year groups
Number and Place Value	 Count to and across 100, forwards and backwards, from 0, 1 or any number. Count, read and write numbers to 100 in numerals. Read and write numbers from 1 to 20 in words. Identify one more and one less than any number (to 100). 	 Read and write numbers from 1 to 20 in numerals Identify one more and one less than any number (to 20) Ordinal numbers (1st, 2nd, 3rd)
Addition and Subtraction	 Be able to work out number bonds to all numbers within 10. Be able to work out number bonds to 10. 	
Multiplication and Division	• Count in 2s to 20, 5s to 50 and 10s to 100.	
Measurement	 Know how many days are in a week Know how many months are in a year. Know when key events happen (eg. Christmas) 	 Know the days of the week in order Know the months of the year in order.
Properties of Shapes		 Recognise and name 2D shapes (rectangles, squares, circles and triangles). Recognise and name 3D shapes (cubes, cuboids, pyramids and spheres).



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Topic	Facts taught in this year group	Facts taught in previous year groups
Number and Place Value	 Count forwards and backwards in 3s from 0. Count forwards and backwards in 10s from any number. 	 Count forwards and backwards in 2s and 5s from 0. Read and write numbers to 100 in numerals.
	 Read and write numbers to 100 in words. Recognise odd and even numbers to 100 	Read and write numbers to 100 in numerals.
Addition and Subtraction		 Know number bonds to all numbers within 10. Know number bonds to 10.
Multiplication and Division	 Know doubles and halves to 20. Know multiplication and division facts for the 2, 5 and 10 times tables. 	• Count in 2s to 20, 5s to 50 and 10s to 100.
Measurement	Know the number of minutes in an hour.Know the number of hours in a day.	Know the value of all coins and notes
Properties of Shapes		 Recognise and name 2D shapes (rectangles, squares, circles and triangles). Recognise and name 3D shapes (cubes, cuboids, pyramids and spheres).



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Topic	Facts taught in this year group	Facts taught in previous year groups
Number and Place Value	 Count, from 0, in 3s to 36, 4s to 48 and 8s to 96. Count in 50s and 100s. Read and write numbers to 1,000 in numerals and words. Know that there are 10 tens = 100. 	Recognise odd and even numbers.
Addition and Subtraction		 Know number bonds to all numbers within 10. Know number bonds to 10.
Multiplication and Division	 Know multiplication and division facts for the 3, 4 and 8 times tables. Divide 10 by 2, 5 and 10 (to support reading scales). 	Know multiplication and division facts for the 2, 5 and 10 times tables.
Fractions	 Count in 10ths. Make a whole from fractions eg. ²/₂, ³/₃ etc. 	
Measurement	 Know the number of seconds in a minute. Know the number of days in each month. Know the number of days in a year and a leap year. 	
Properties of Shapes		 Recognise and name 2D shapes (rectangles, squares, circles and triangles). Recognise and name 3D shapes (cubes, cuboids, pyramids and spheres).



Торіс	Facts taught in this year group	Facts taught in previous year groups
Number and Place	• Count in 25s and 1,000s.	Recognise odd and even numbers.
Value	• Know 10 hundreds = 1,000.	
Addition and		Know number bonds to all numbers within 10.
Subtraction		Know number bonds to 10.
Multiplication and Division	 Know multiplication and division facts for all times tables to 12 x 12. Divide 1,000 by 2, 4, 5, 10 (to support reading 	 Know multiplication and division facts for 2, 5, 10, 3, 4 and 8 times tables.
	scales).	
Fractions	• Count in 100ths.	
	• Recognise and write decimal equivalents to $\frac{1}{4}$, $\frac{1}{2}$ and $\frac{3}{4}$.	
Measurement	Know that:	
	> 1cm = 10mm	
	> 1m = 100cm	
	> 1km = 1000m	
	> 1kg = 1000g	
	> 1L = 1000ml	
	• Know that:	
	> 1hr = 60 minutes	
	> 1 min = 60 seconds	
	> 1 year = 12 months	
	> 1 week = 7 days	



Topic	Facts taught in this year group	Facts taught in previous year groups
Number and Place Value	Recognise odd and even numbers.	
	• Know that:	
	> 10 tenths = 1	
	> 100 hundredths = 1	
	> 10 hundredths = 1 tenth	
Addition and		 Know number bonds to all numbers within 10.
Subtraction		 Know number bonds to 10.
Multiplication and	Know prime number to 19.	Know multiplication and division facts for all times
Division	• Know square numbers to 12 ² .	tables to 12 \times 12.
	• Divide 1 by 2, 4, 5 and 10 (to support reading	
	scales).	
Fractions	Know percentage and decimal equivalents to	
	$\frac{1}{2}, \frac{1}{4}, \frac{1}{5}, \frac{2}{5}, \frac{4}{5}$ and fractions with denominators that are	
	multiples of 10 and 25.	
Measurement		Know that:
		> 1cm = 10mm
		> 1m = 100cm
		> 1km = 1000m
		> 1kg = 1000g
		> 1L = 1000ml
		Know that:
		> 1hr = 60 minutes
		> 1 min = 60 seconds
		> 1 year = 12 months

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Topic	Facts taught in this year group	Facts taught in previous year groups
Number and Place Value		Recognise odd and even numbers.
4 Operations	 Know the order of operations (BIDMAS). Divide 1, 10, 100 and 1,000 by 2, 4, 5 and 10 (to support reading scales). 	 Know number bonds to all numbers within 10. Know number bonds to 10. Know multiplication and division facts for all times tables to 12 x 12. Know prime number to 19. Know square numbers to 12².
Fractions	• Know percentage and decimal equivalents to $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{5}$, $\frac{2}{5}$. $\frac{4}{5}$ and fractions with denominators that are multiples of 10 and 25.	
Measurement	• Know that: > 8km = 5 miles	 Know that: 1cm = 10mm 1m = 100cm 1km = 1000m 1kg = 1000g 1L = 1000ml Know that: 1hr = 60 minutes 1 min = 60 seconds 1 year = 12 months

	KEW RIVERSIDE PRIMARY	> 1 week = 7 days
Properties of Shapes	Know the names of all parts of a circle (radius,	• Know that there are 360° in a full turn.
	diameter, circumference).	Know that there are 180° on a straight line.
	Know that the diameter is double the radius.	
	Know that the radius is half the diameter.	